### Forecasting an Origin-Destination (OD) Distribution

#### Image of OD distribution



#### OD matrix (distribution)

	Zone 1	Zone 2	Zone 3	Sum
Zone 1	X <sub>11</sub>	X <sub>12</sub>	X <sub>13</sub>	O <sub>1</sub>
Zone 2	X <sub>21</sub>	X <sub>22</sub>	X <sub>23</sub>	O <sub>2</sub>
Zone 3	X <sub>31</sub>	X <sub>32</sub>	X <sub>33</sub>	O <sub>3</sub>
sum	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	

## Approach : a set of OD matrix

Previous studies obtain *"one"* OD matrix which has the highest likelihood and utilize the OD matrix for road planning.





I try to obtain a set of OD matrix which show a distribution of OD matrix.

- Only one estimated OD matrix cannot correspond to a real one.
- A set of calculated OD matrices can contain a real one.
- Apply a Monte Carlo sampling and Get a distribution of OD matrix.



### Destination choice & Sampling

• Individual at zone *i* choose their destination *j* according to:

$$\sum_{\text{probability}}^{\text{Destination choice}} p_{i \to j} = \frac{\exp(G_j + \nu_{i \to j} + c_{i \to j})}{\sum_{\forall j} \exp(G_j + \nu_{i \to j} + c_{i \to j})}$$

 $G_j$ : observed utility (attractiveness of destination j)  $c_{i \rightarrow j}$ : travel cost  $v_{i \rightarrow j}$ : unobserved spatial variation and given by normal distribution

• Total departure volume and probability  $p_{i \rightarrow j}$  give  $X_{i \rightarrow j}$ 

[Application : Monte Calro method, Alias method]

• One OD matrix is obtained by this process in all zones and I apply iterative calculation to obtain many OD matrix



#### Convergence process

- Attractiveness  $G_i$  and travel cost  $c_{i \rightarrow j}$  are related to a OD matrix
- Need a convergence of  $G_j$ ,  $c_{i \rightarrow j}$  and  $X_{i \rightarrow j}$



• To obtain  $G_i$ , I need to solve non-linear simultaneous equations

$$f_j(\boldsymbol{G}) = D_j - \sum_i E[X_{ij}(\boldsymbol{G})], \forall j$$

[Application : quasi-Newton method, numerical differentiation]

# Travel cost (user equilibrium approach)

Equilibrium state (Wardrop's first principle  $\cong$  Nash equilibrium) :

- Drivers should prefer a fastest route
- All drivers successfully choose shortest routes for them in a final situation

Traffic assignment method (Franc-Wolfe method)

- Shortest path serach
- Line search (all-or-nothing approach)



Link: 40,003 Node: 13,389 OD: 18,503,872