

MPI Programming

IHPCSS

Communicators

July 7-12, 2019

PRESENTED BY:

John Cazes

cazes@tacc.utexas.edu

Outline

Advantages of Message Passing

Background on MPI

Basic Information

Point to Point Communication

Nonblocking Communication

Wildcards

Probing

Collective Communications

"V" Operations

Derived Datatypes

Communicators

Communicators

A communicator is a “[context](#)” for communicating only among a group of tasks.

[**MPI_COMM_WORLD**](#) is the default communicator and consists of all tasks.

Communication is isolated to [context of the group](#)— i.e. no messages from other contexts are “seen”.

New communicators are formed recursively from [**MPI_COMM_WORLD**](#).

Why Communicators?

Isolate communication to a small number of processors

Useful for creating libraries

Collective communication between subgroups (in lieu of all tasks) can drastically reduce communication costs if only some need to participate

Useful for communicating with "nearest neighbors"

Duplication

Simplest new communicator: identical to a previous one.

```
MPI_Comm_dup(MPI_Comm comm, MPI_Comm *newcomm)
```

This is useful for library writers:

```
MPI_Isend(...); MPI_Irecv(...);  
// library call  
MPI_Waitall(...);
```

Groups, Contexts, Communicators

- Group: An ordered set of processes, each associated with a rank (within a continuous range).
- Context: A property of a communicator that partitions the communication space.
 - Not externally visible.
 - Contexts allow Pt2Pt and collective calls not to interfere with each other.
- Communicator: Group + Context + other info
 - context that differentiates one communicator from another
 - group of processes contained by the communicator
 - Predefined: MPI_COMM_WORLD,MPI_COMM_SELF

Groups

A new communication group can only be created from a previously defined group. A group must also have a context for communication and, therefore, must have a communicator created for it. The basic steps to form a group are:

Obtain a complete set of task IDs from a communicator
[`MPI_Comm_group`](#).

Create a group as a subset of the complete set by
[`MPI_Group_excl`](#), [`MPI_Group_incl`](#), ...

Create the new communicator for group (subset) using
[`MPI_Comm_create`](#).

Group Constructors

Routine	Function
<code>MPI_Comm_group</code>	returns group reference of a communicator
<code>MPI_Group_incl</code>	forms new group from inclusion list
<code>MPI_Group_excl</code>	forms new group from exclusion list
<code>MPI_Group_{union, intersection, difference}</code>	Forms new group from union, intersection, or difference of 2 groups.
<code>MPI_Comm_create</code>	creates communicator from a group reference

Group Constructors

```
MPI_Comm_group(MPI_Comm comm, MPI_Group *group)
```

```
MPI_Group_union(MPI_Group group1, MPI_Group group2, MPI_Group *newgroup)
```

```
MPI_Group_intersection(MPI_Group group1, MPI_Group group2, MPI_Group *newgroup)
```

```
MPI_Group_difference(MPI_Group group1, MPI_Group group2, MPI_Group *newgroup)
```

```
MPI_Group_incl(MPI_Group group, int n, int *ranks, MPI_Group *newgroup)
```

```
MPI_Group_excl(MPI_Group group, int n, int *ranks, MPI_Group *newgroup)
```

```
MPI_Group_range_incl(MPI_Group group, int n, int ranges[][3], MPI_Group *newgroup)
```

```
MPI_Group_range_excl(MPI_Group group, int n, int ranges[][3], MPI_Group *newgroup)
```

Master/Worker C Example

```
main(int argc, char **argv) {
    int my_PE, send_data=1, recv_data1, recv_data2;
    MPI_Group group_world, group_worker;
    MPI_Comm comm_worker;
    int ranks[] = {0};
    //Ranks to exclude, just 0 here
    MPI_Init(&argc, &argv);
    MPI_Comm_rank(MPI_COMM_WORLD, &my_PE);
    MPI_Comm_group(MPI_COMM_WORLD, &group_world);
    MPI_Group_excl(group_world, 1, ranks, &group_worker);
    MPI_Comm_create(MPI_COMM_WORLD, group_worker, &comm_worker);
    //Reduce just for workers
    if(my_PE != 0)
        MPI_Reduce(&send_data, &recv_data1, 1, MPI_INT, MPI_SUM, 0,
comm_worker);
        MPI_Reduce(&send_data, &recv_data2, 1, MPI_INT, MPI_SUM, 0,
MPI_COMM_WORLD);
    //Proper clean up
    if (comm_worker != MPI_COMM_NULL)
        MPI_Comm_free(&comm_worker); //comm_worker is NULL on PE 0
    MPI_Group_free(&group_world); MPI_Group_free(&group_worker);
    MPI_Finalize(); }
```

Creating Communicators for Groups

```
#include <mpi.h>
#include <stdio.h>
#include <stdlib.h>
#define MAXEVEN 128
main(int argc, char **argv) {
    int npes, irank, ierr;
    int neven, iegid, iogid, i, iranks[MAXEVEN];

    MPI_Group iegroup, iogroup, iwgroup;
    MPI_Comm iecomm, iocomm;

    ierr = MPI_Init(&argc, &argv);
    ierr = MPI_Comm_size(MPI_COMM_WORLD, &npes);
    ierr = MPI_Comm_rank(MPI_COMM_WORLD, &irank);

    /* Extract group from World Comm. */

    ierr = MPI_Comm_group(MPI_COMM_WORLD, &iwgroup);
```

Creating Communicators for Groups

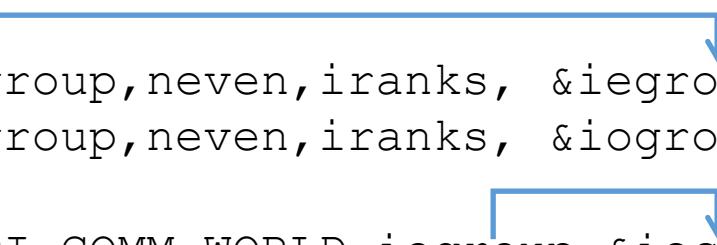
```
        /* Make list of even ranks. */

neven = (npes+1)/2;
if(neven > MAXEVEN) exit(1);
for(i=0; i < npes; i+=2) iranks[i/2] = i;

        /* Form even and odd groups. */

ierr = MPI_Group_incl(iwgroup,neven,iranks, &iegroup);
ierr = MPI_Group_excl(iwgroup,neven,iranks, &iogroup);

ierr = MPI_Comm_create(MPI_COMM_WORLD,iegroup,&iecomm);
ierr = MPI_Comm_create(MPI_COMM_WORLD,iogroup,&iocomm);
```



Creating Communicators for Groups

```
ierr = MPI_Group_rank(iegroup, &iegid);
if(iegid != MPI_UNDEFINED) {
    printf("PE: %d, id %d of even group.\n", irank, iegid);
}
else {
    ierr = MPI_Group_rank(iogroup, &iogid);
    printf("PE: %d, id %d of odd group.\n", irank, iogid);
}
MPI_Comm_free( iecomm ); MPI_Comm_free( iocomm );
MPI_Group_free(iegroup); MPI_Group_free(iogroup);

ierr = MPI_Finalize();
}
```

MPI_Comm_split

Provides a short cut method to create a collection of communicators

All processors with the "same color" will be in the same communicator

Index controls relative rank in group

Fortran

```
MPI_Comm_split(OLD_COMM, color, index, NEW_COMM, ierr)
```

C

```
MPI_Comm_split(OLD_COMM, color, index, &NEW_COMM)
```

MPI_Comm_split

```
call MPI_Comm_rank(MPI_COMM_WORLD, irank, ierr)
icolor = modulo(irank, 3)
key    = npes - irank/3 ! reverse the ordering

call MPI_Comm_split(MPI_COMM_WORLD, icolor, key, newcom, ierr)
call MPI_Comm_rank(newcom,mysrank, ierr)

psum = irank
call MPI_Reduce(psum,tot,1,MPI_INTEGER,MPI_SUM,0,newcom,ierr)
print*, irank,icolor,key,mysrank,tot
```

Color 0	0	0	9	2	0
Color 1	1	1	9	2	0
Color 2	2	2	9	2	0
	3	0	8	1	0
	4	1	8	1	0
	5	2	8	1	0
	6	0	7	0	9
	7	1	7	0	12
	8	2	7	0	15

Colors are 0, 1 and 2
Keys are 9, 8 and 7
Lowest keys are roots

(Virtual) Topologies

In terms of MPI, a virtual topology **describes a mapping and ordering of MPI processes into a geometric shape.**

The two main types of topology supported by MPI are **Cartesian**(grid) and **Graph**.

MPI topologies are **virtual – there may be no relation between the physical structure of parallel machine and the process topology.**

Virtual topologies are **built upon MPI communicator and groups.**

Must be **built by the application developer.**

Useful for applications with **specific communication pattern.**

A particular **implementation may optimize process mapping** based on the physical characteristics of a given parallel machine.

Topologies

Use the MPI library for common grid topologies (**local functions**)

A *topology* maps each rank onto a set of N-tuples (N dimensions)

E.g. For a 2x2 Cartesian grid:

Ranks:{**0**, **1**, **2**, **3**}->{(0,0), (0,1),
(1,0), (1,1)} tuples (row-major in ranks)

Cartesian map operations:

[MPI_Cart_create](#)

Creates map (ranks → coordinates).

[MPI_Cart_get](#)

Returns info created in MPI_Cart_create.

[MPI_Cart_coords](#)

Returns coordinates from rank.

[MPI_Cart_rank](#)

Returns rank from coordinates.

[MPI_Cart_shift](#)

Returns rank of neighbors in nth dimension.

Note: the virtual topology does not necessarily map the hardware processor grid
to the process grid in the most efficient manner.

Topologies

Use Case:

1. Build 2-/3-D Cartesian Grid
2. Use shift operator to get neighbor rank
for destination and source
in x, y and z directions

Creating a Cartesian Topology

```
C: int MPI_Cart_create(MPI_Comm comm_old,  
                      int ndims, int *dims, int *periods,  
                      int reorder, MPI_Comm *comm_cart)
```

```
Fortran: MPI_CART_CREATE(COMM_OLD, NDIMS, DIMS,  
                         PERIODS, REORDER, COMM_CART, IERROR)  
INTEGER COMM_OLD, NDIMS, DIMS(*), COMM_CART, IERROR  
LOGICAL PERIODS(*), REORDER
```

comm_old: [in] input communicator
ndims: [in] number of dimensions of cartesian grid
dims: [in] number of processes in each dimension (size ndims)
periods: [in] grid is periodic or not in each dimension (size ndims)
reorder: [in] ranking may be reordered or not
comm_cart:[out]communicator with new cartesian topology

Balanced Processor Distribution

C: int **MPI_Dims_create**(int nnodes, int ndims, int *dims)

Fortran: **MPI_DIMS_CREATE**(NNODES, NDIMS, DIMS, IERROR)

INTEGER NNODES, NDIMS, DIMS(*), IERROR

nnodes: [in] number of nodes in a grid

ndims: [in] number of cartesian dimensions

dims: [in/out] number of nodes in each dimension (size ndims)

- Call tries to set dimensions as close to each other as possible
- Non-zero values in dims will not be changed

dims before call	function call	dims on return
(0, 0)	<code>MPI_DIMS_CREATE(6, 2, dims)</code>	(3, 2)
(0, 0)	<code>MPI_DIMS_CREATE(7, 2, dims)</code>	(7, 1)
(0, 3, 0)	<code>MPI_DIMS_CREATE(6, 3, dims)</code>	(2, 3, 1)
(0, 3, 0)	<code>MPI_DIMS_CREATE(7, 3, dims)</code>	erroneous call

Cartesian Query Functions

Library support and convenience!

- `MPI_Cartdim_get`(comm_cart, ndims)
 - Gets dimensions of a Cartesian communicator
- `MPI_Cart_get`(comm_cart, ndims, dims, periods, coords)
 - Gets size of dimensions
 - `coords`: coordinates of calling process in cartesian structure (array of integer)
- `MPI_Cart_rank`(comm_cart, coords, rank)
 - Translate coordinates to rank
- `MPI_Cart_coords`(comm_cart, rank, ndims, coords)
 - Translate rank to coordinates

Topologies (Shift)

C

```
MPI_Cart_shift(comm_cart, direct, disp, &rank_src, &rank_dst)
```

Fortran

```
MPI_Cart_shift(comm_cart, direct, disp, rank_src, rank_dst, ierr)
```

Parameters

comm_cart: communicator with Cartesian structure

direct : coordinate dimension of shift

disp : >0 = upwards shift, <0 = downwards shift

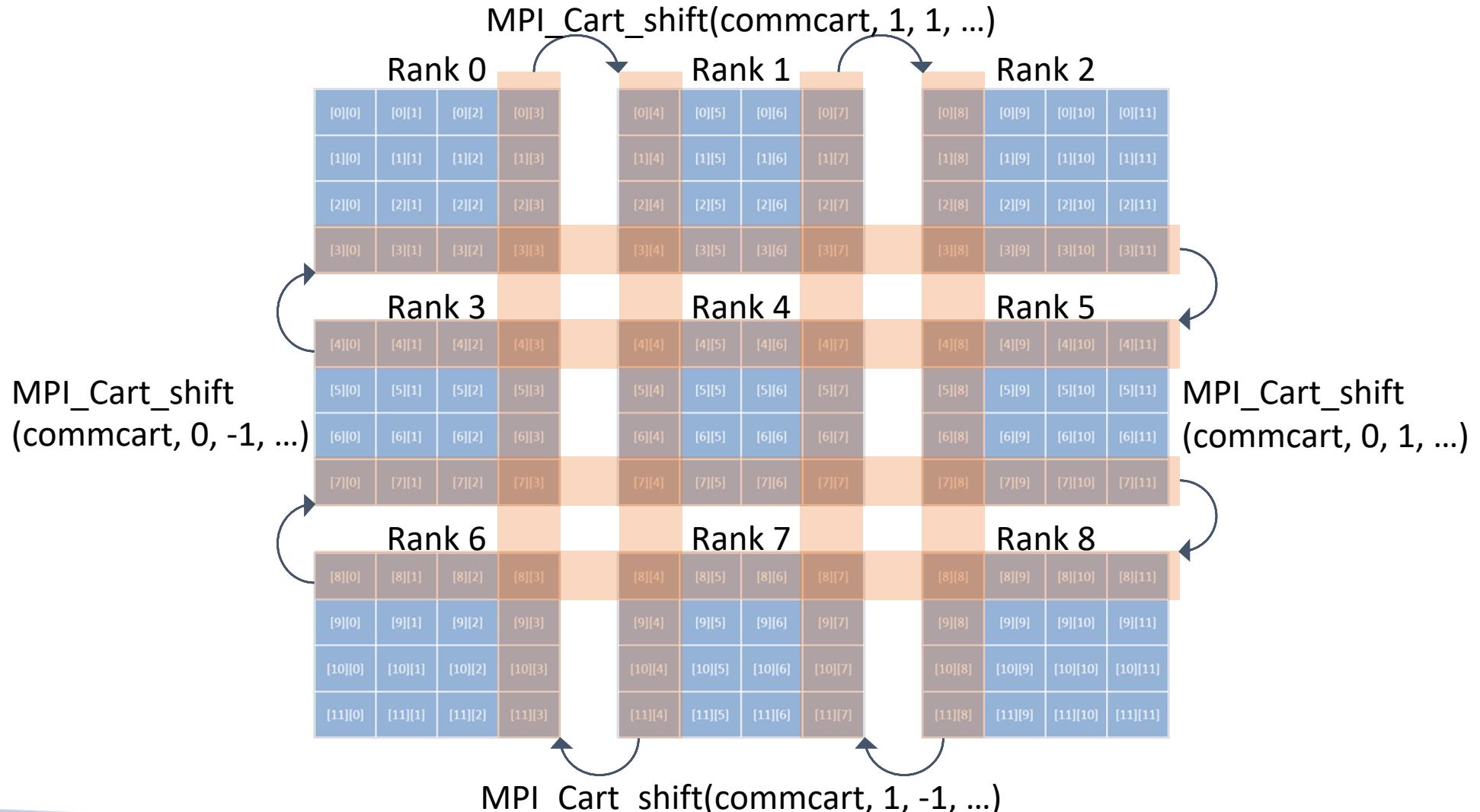
end-off/circular shift (see periods of MPI_Cart_create)

rank_src : output: rank of source process

rank_dst : output: rank of destination process

MPI_PROC_NULL for shifts at non-periodic boundaries

Shift Example (non-periodic)



Topology Illustrations

Rank map onto 2-D Cartesian Topology

0 (0, 0)	1 (0, 1)	2 (0, 2)
3 (1, 0)	4 (1, 1)	5 (1, 2)
6 (2, 0)	7 (2, 1)	8 (2, 2)

Column/Row Shift (periodic)

Periodic Displacement of 1 in Dimension “0”

Row Shift

B _{0,0}	B _{0,1}	B _{0,2}
B _{1,0}	B _{1,1}	B _{1,2}
B _{2,0}	B _{2,1}	B _{2,2}

B _{1,0}	B _{1,1}	B _{1,2}
B _{2,0}	B _{2,1}	B _{2,2}
B _{0,0}	B _{0,1}	B _{0,2}

rank_dst =

B _{2,0}	B _{2,1}	B _{2,2}
B _{0,0}	B _{0,1}	B _{0,2}
B _{1,0}	B _{1,1}	B _{1,2}

rank_src =

Periodic Displacement of 1 in Dimension “1”

Column Shift

A _{0,0}	A _{0,1}	A _{0,2}
A _{1,0}	A _{1,1}	A _{1,2}
A _{2,0}	A _{2,1}	A _{2,2}

rank_dst =

A _{0,1}	A _{0,2}	A _{0,0}
A _{1,1}	A _{1,2}	A _{1,0}
A _{2,1}	A _{2,2}	A _{2,0}

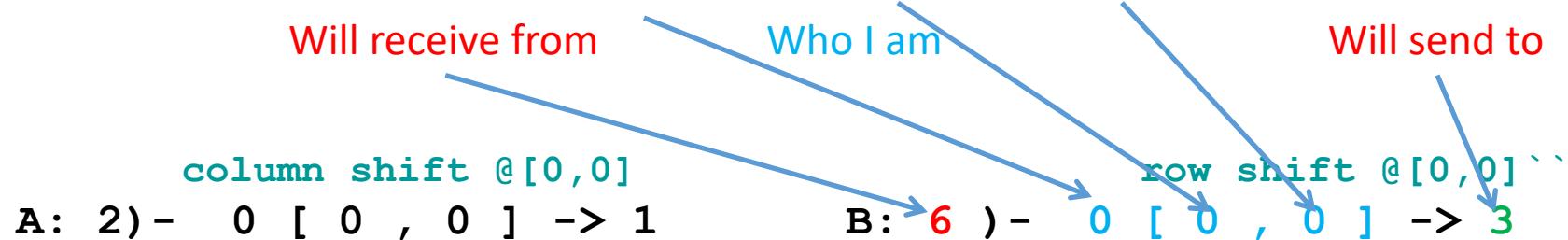
rank_src =

A _{0,2}	A _{0,0}	A _{0,1}
A _{1,2}	A _{1,0}	A _{1,1}
A _{2,2}	A _{2,0}	A _{2,1}

Fortran Example

```
integer,parameter :: NP=3
logical, dimension(2)    :: lvper=(/.true.,.true./), lvperx
integer, dimension(2)    :: ivdim=(/      NP,      NP/), ivdimx
integer, dimension(2)    :: mygrid
...
call MPI_Cart_create(iwcomm,2,ivdim ,lvper, .false.,igcomm,ir)
call MPI_Cart_get( igcomm,2,ivdimx,lvperx, mygrid, ir)
call MPI_Cart_shift( igcomm,1,1, isrc,ides, ierr)
call MPI_Cart_shift( igcomm,0,1, isrcb,idesb, ierr)
myrow=mygrid(1);mycol=mygrid(2);mype=rank
```

```
print*, 'A:',isrc,'-',mype,['',myrow,'','mycol,'] ->',ides,
& '          B:',isrcb,'-',mype,['',myrow,'','mycol,'] ->',idesb
```



C Example

```
#include <mpi.h>
#include <stdio.h>
#define NP 3

main(int argc, char **argv) {
    int npes,      mype, ierr,   myrow, mycol;
    int isrca,    isrcb, idesa, idesb;
    MPI_Comm IWCOMM = MPI_COMM_WORLD, igcomm;
/*  MPI Cartesian Grid information */
    int ivdim[2] = {NP,NP}, ivper[2]={1,1};
    int ivdimx[2],           ivperx[2], mygrids[2];
...
/*  Create Cartesian Grid and extract information */

    ierr= MPI_Cart_create(IWCOMM,2,ivdim ,ivper, 0,&igcomm);
    ierr= MPI_Cart_get(    igcomm,2,ivdimx,ivperx, mygrids);
    ierr= MPI_Cart_shift( igcomm,1,1, &isrca,&idesa);
    ierr= MPI_Cart_shift( igcomm,0,1, &isrcb,&idesb);
```

Generic Example: Send “a” blocks down, and “b” blocks right.

```
MPI_CART_SHIFT(cartcomm, 0, 1, UP, DOWN )
MPI_CART_SHIFT(cartcomm, 1, 1, LEFT, RIGHT )

...
MPI_ISEND(a1, N,MPI_INTEGER, DOWN, 1,MPI_COMM_WORLD,reqa1 )
MPI_IRecv(a2, N,MPI_INTEGER, UP, 1,MPI_COMM_WORLD,reqa2 )

...
MPI_ISEND(b1, N,MPI_INTEGER, RIGHT, 2,MPI_COMM_WORLD,reqb1 )
MPI_IRecv(b2, N,MPI_INTEGER, LEFT, 2,MPI_COMM_WORLD,reqb2 )
```

Cartesian subspaces

Rank 0	Rank 1	Rank 2
[0][0] [0][1] [0][2] [0][3]	[0][4] [0][5] [0][6] [0][7]	[0][8] [0][9] [0][10] [0][11]
[1][0] [1][1] [1][2] [1][3]	[1][4] [1][5] [1][6] [1][7]	[1][8] [1][9] [1][10] [1][11]
[2][0] [2][1] [2][2] [2][3]	[2][4] [2][5] [2][6] [2][7]	[2][8] [2][9] [2][10] [2][11]
[3][0] [3][1] [3][2] [3][3]	[3][4] [3][5] [3][6] [3][7]	[3][8] [3][9] [3][10] [3][11]

Rank 3	Rank 4	Rank 5
[4][0] [4][1] [4][2] [4][3]	[4][4] [4][5] [4][6] [4][7]	[4][8] [4][9] [4][10] [4][11]
[5][0] [5][1] [5][2] [5][3]	[5][4] [5][5] [5][6] [5][7]	[5][8] [5][9] [5][10] [5][11]
[6][0] [6][1] [6][2] [6][3]	[6][4] [6][5] [6][6] [6][7]	[6][8] [6][9] [6][10] [6][11]
[7][0] [7][1] [7][2] [7][3]	[7][4] [7][5] [7][6] [7][7]	[7][8] [7][9] [7][10] [7][11]

Rank 6	Rank 7	Rank 8
[8][0] [8][1] [8][2] [8][3]	[8][4] [8][5] [8][6] [8][7]	[8][8] [8][9] [8][10] [8][11]
[9][0] [9][1] [9][2] [9][3]	[9][4] [9][5] [9][6] [9][7]	[9][8] [9][9] [9][10] [9][11]
[10][0] [10][1] [10][2] [10][3]	[10][4] [10][5] [10][6] [10][7]	[10][8] [10][9] [10][10] [10][11]
[11][0] [11][1] [11][2] [11][3]	[11][4] [11][5] [11][6] [11][7]	[11][8] [11][9] [11][10] [11][11]

```
MPI_Cart_sub (comm_cart, remain_dims, comm_sub)
{1, 0}
(true, false)
```

Cartesian subspaces

Rank 0	Rank 1	Rank 2																																																
<table><tbody><tr><td>[0][0]</td><td>[0][1]</td><td>[0][2]</td><td>[0][3]</td></tr><tr><td>[1][0]</td><td>[1][1]</td><td>[1][2]</td><td>[1][3]</td></tr><tr><td>[2][0]</td><td>[2][1]</td><td>[2][2]</td><td>[2][3]</td></tr><tr><td>[3][0]</td><td>[3][1]</td><td>[3][2]</td><td>[3][3]</td></tr></tbody></table> 0	[0][0]	[0][1]	[0][2]	[0][3]	[1][0]	[1][1]	[1][2]	[1][3]	[2][0]	[2][1]	[2][2]	[2][3]	[3][0]	[3][1]	[3][2]	[3][3]	<table><tbody><tr><td>[0][4]</td><td>[0][5]</td><td>[0][6]</td><td>[0][7]</td></tr><tr><td>[1][4]</td><td>[1][5]</td><td>[1][6]</td><td>[1][7]</td></tr><tr><td>[2][4]</td><td>[2][5]</td><td>[2][6]</td><td>[2][7]</td></tr><tr><td>[3][4]</td><td>[3][5]</td><td>[3][6]</td><td>[3][7]</td></tr></tbody></table> 0	[0][4]	[0][5]	[0][6]	[0][7]	[1][4]	[1][5]	[1][6]	[1][7]	[2][4]	[2][5]	[2][6]	[2][7]	[3][4]	[3][5]	[3][6]	[3][7]	<table><tbody><tr><td>[0][8]</td><td>[0][9]</td><td>[0][10]</td><td>[0][11]</td></tr><tr><td>[1][8]</td><td>[1][9]</td><td>[1][10]</td><td>[1][11]</td></tr><tr><td>[2][8]</td><td>[2][9]</td><td>[2][10]</td><td>[2][11]</td></tr><tr><td>[3][8]</td><td>[3][9]</td><td>[3][10]</td><td>[3][11]</td></tr></tbody></table> 0	[0][8]	[0][9]	[0][10]	[0][11]	[1][8]	[1][9]	[1][10]	[1][11]	[2][8]	[2][9]	[2][10]	[2][11]	[3][8]	[3][9]	[3][10]	[3][11]
[0][0]	[0][1]	[0][2]	[0][3]																																															
[1][0]	[1][1]	[1][2]	[1][3]																																															
[2][0]	[2][1]	[2][2]	[2][3]																																															
[3][0]	[3][1]	[3][2]	[3][3]																																															
[0][4]	[0][5]	[0][6]	[0][7]																																															
[1][4]	[1][5]	[1][6]	[1][7]																																															
[2][4]	[2][5]	[2][6]	[2][7]																																															
[3][4]	[3][5]	[3][6]	[3][7]																																															
[0][8]	[0][9]	[0][10]	[0][11]																																															
[1][8]	[1][9]	[1][10]	[1][11]																																															
[2][8]	[2][9]	[2][10]	[2][11]																																															
[3][8]	[3][9]	[3][10]	[3][11]																																															
Rank 3	Rank 4	Rank 5																																																
<table><tbody><tr><td>[4][0]</td><td>[4][1]</td><td>[4][2]</td><td>[4][3]</td></tr><tr><td>[5][0]</td><td>[5][1]</td><td>[5][2]</td><td>[5][3]</td></tr><tr><td>[6][0]</td><td>[6][1]</td><td>[6][2]</td><td>[6][3]</td></tr><tr><td>[7][0]</td><td>[7][1]</td><td>[7][2]</td><td>[7][3]</td></tr></tbody></table> 1	[4][0]	[4][1]	[4][2]	[4][3]	[5][0]	[5][1]	[5][2]	[5][3]	[6][0]	[6][1]	[6][2]	[6][3]	[7][0]	[7][1]	[7][2]	[7][3]	<table><tbody><tr><td>[4][4]</td><td>[4][5]</td><td>[4][6]</td><td>[4][7]</td></tr><tr><td>[5][4]</td><td>[5][5]</td><td>[5][6]</td><td>[5][7]</td></tr><tr><td>[6][4]</td><td>[6][5]</td><td>[6][6]</td><td>[6][7]</td></tr><tr><td>[7][4]</td><td>[7][5]</td><td>[7][6]</td><td>[7][7]</td></tr></tbody></table> 1	[4][4]	[4][5]	[4][6]	[4][7]	[5][4]	[5][5]	[5][6]	[5][7]	[6][4]	[6][5]	[6][6]	[6][7]	[7][4]	[7][5]	[7][6]	[7][7]	<table><tbody><tr><td>[4][8]</td><td>[4][9]</td><td>[4][10]</td><td>[4][11]</td></tr><tr><td>[5][8]</td><td>[5][9]</td><td>[5][10]</td><td>[5][11]</td></tr><tr><td>[6][8]</td><td>[6][9]</td><td>[6][10]</td><td>[6][11]</td></tr><tr><td>[7][8]</td><td>[7][9]</td><td>[7][10]</td><td>[7][11]</td></tr></tbody></table> 1	[4][8]	[4][9]	[4][10]	[4][11]	[5][8]	[5][9]	[5][10]	[5][11]	[6][8]	[6][9]	[6][10]	[6][11]	[7][8]	[7][9]	[7][10]	[7][11]
[4][0]	[4][1]	[4][2]	[4][3]																																															
[5][0]	[5][1]	[5][2]	[5][3]																																															
[6][0]	[6][1]	[6][2]	[6][3]																																															
[7][0]	[7][1]	[7][2]	[7][3]																																															
[4][4]	[4][5]	[4][6]	[4][7]																																															
[5][4]	[5][5]	[5][6]	[5][7]																																															
[6][4]	[6][5]	[6][6]	[6][7]																																															
[7][4]	[7][5]	[7][6]	[7][7]																																															
[4][8]	[4][9]	[4][10]	[4][11]																																															
[5][8]	[5][9]	[5][10]	[5][11]																																															
[6][8]	[6][9]	[6][10]	[6][11]																																															
[7][8]	[7][9]	[7][10]	[7][11]																																															
Rank 6	Rank 7	Rank 8																																																
<table><tbody><tr><td>[8][0]</td><td>[8][1]</td><td>[8][2]</td><td>[8][3]</td></tr><tr><td>[9][0]</td><td>[9][1]</td><td>[9][2]</td><td>[9][3]</td></tr><tr><td>[10][0]</td><td>[10][1]</td><td>[10][2]</td><td>[10][3]</td></tr><tr><td>[11][0]</td><td>[11][1]</td><td>[11][2]</td><td>[11][3]</td></tr></tbody></table> 2	[8][0]	[8][1]	[8][2]	[8][3]	[9][0]	[9][1]	[9][2]	[9][3]	[10][0]	[10][1]	[10][2]	[10][3]	[11][0]	[11][1]	[11][2]	[11][3]	<table><tbody><tr><td>[8][4]</td><td>[8][5]</td><td>[8][6]</td><td>[8][7]</td></tr><tr><td>[9][4]</td><td>[9][5]</td><td>[9][6]</td><td>[9][7]</td></tr><tr><td>[10][4]</td><td>[10][5]</td><td>[10][6]</td><td>[10][7]</td></tr><tr><td>[11][4]</td><td>[11][5]</td><td>[11][6]</td><td>[11][7]</td></tr></tbody></table> 2	[8][4]	[8][5]	[8][6]	[8][7]	[9][4]	[9][5]	[9][6]	[9][7]	[10][4]	[10][5]	[10][6]	[10][7]	[11][4]	[11][5]	[11][6]	[11][7]	<table><tbody><tr><td>[8][8]</td><td>[8][9]</td><td>[8][10]</td><td>[8][11]</td></tr><tr><td>[9][8]</td><td>[9][9]</td><td>[9][10]</td><td>[9][11]</td></tr><tr><td>[10][8]</td><td>[10][9]</td><td>[10][10]</td><td>[10][11]</td></tr><tr><td>[11][8]</td><td>[11][9]</td><td>[11][10]</td><td>[11][11]</td></tr></tbody></table> 2	[8][8]	[8][9]	[8][10]	[8][11]	[9][8]	[9][9]	[9][10]	[9][11]	[10][8]	[10][9]	[10][10]	[10][11]	[11][8]	[11][9]	[11][10]	[11][11]
[8][0]	[8][1]	[8][2]	[8][3]																																															
[9][0]	[9][1]	[9][2]	[9][3]																																															
[10][0]	[10][1]	[10][2]	[10][3]																																															
[11][0]	[11][1]	[11][2]	[11][3]																																															
[8][4]	[8][5]	[8][6]	[8][7]																																															
[9][4]	[9][5]	[9][6]	[9][7]																																															
[10][4]	[10][5]	[10][6]	[10][7]																																															
[11][4]	[11][5]	[11][6]	[11][7]																																															
[8][8]	[8][9]	[8][10]	[8][11]																																															
[9][8]	[9][9]	[9][10]	[9][11]																																															
[10][8]	[10][9]	[10][10]	[10][11]																																															
[11][8]	[11][9]	[11][10]	[11][11]																																															

```
MPI_Cart_sub (comm_cart, remain_dims, comm_sub)
{ 0, 1 }
(false, true)
```

Outline

Advantages of Message Passing

Background on MPI

Basic Information

Point to Point Communication

Nonblocking Communication

Wildcards

Probing

Collective Communications

"V" Operations

Derived Datatypes

Communicators

License

©The University of Texas at Austin, 2019

This work is licensed under the Creative Commons Attribution Non-Commercial 3.0 Unported License. To view a copy of this license, visit <http://creativecommons.org/licenses/by-nc/3.0/>

When attributing this work, please use the following text: “Introduction to Many Core Programming”, Texas Advanced Computing Center, 2018. Available under a Creative Commons Attribution Non-Commercial 3.0 Unported License.

