

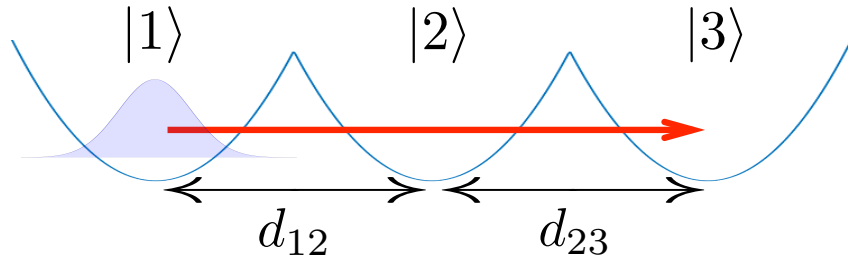
A boson dispensing machine

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We present a technique to control the spatial state of a small cloud of interacting bosons at low temperatures with almost perfect fidelity using spatial adiabatic passage. To achieve this, the resonant trap energies of the system are engineered in such a way that a single, well-defined eigenstate connects the initial and desired states and is isolated from the rest of the spectrum. We apply this procedure to the task of separating a well-defined number of particles from an initial cloud and show that it can be implemented in radio-frequency traps using experimentally realistic parameters.



Single particle Spatial Adiabatic Passage



The Hamiltonian:

$$\hat{H}(t) = \hbar \begin{pmatrix} 0 & \Omega_{12}(t) & 0 \\ \Omega_{12}(t) & 0 & \Omega_{23}(t) \\ 0 & \Omega_{23}(t) & 0 \end{pmatrix}$$

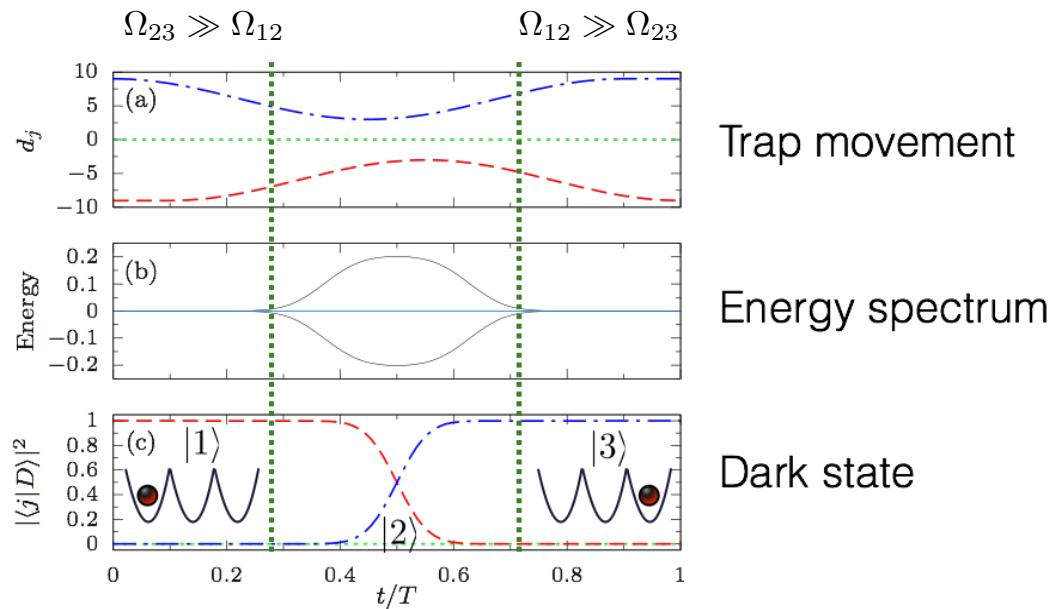
The process must be slow enough to follow the eigenstate (adiabatic).

The initial and the final states must be resonant.

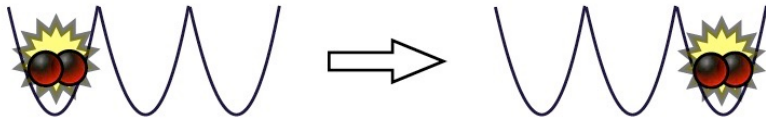
Existence of the “dark state”:

$$|D\rangle = \cos \theta |L\rangle - \sin \theta |R\rangle, \quad \tan \theta = \frac{\Omega_{LM}(d_{LM})}{\Omega_{MR}(d_{MR})}$$

$$|L\rangle = |1\rangle, |M\rangle = |2\rangle, |R\rangle = |3\rangle$$



Two-boson Spatial Adiabatic Passage

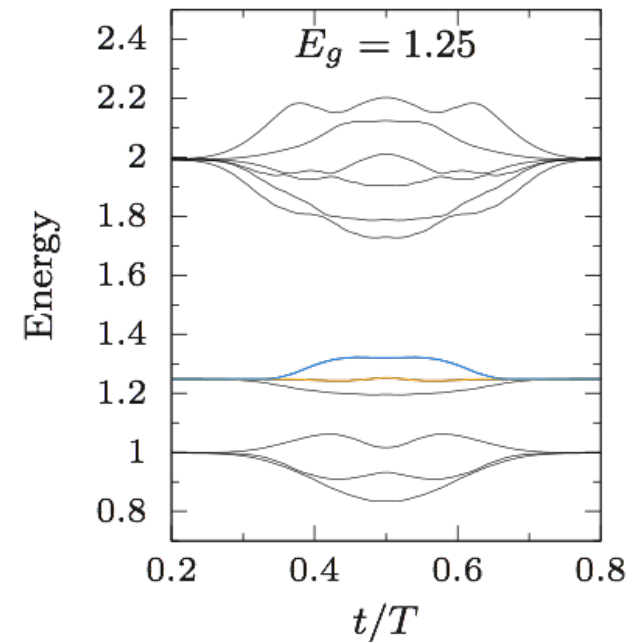
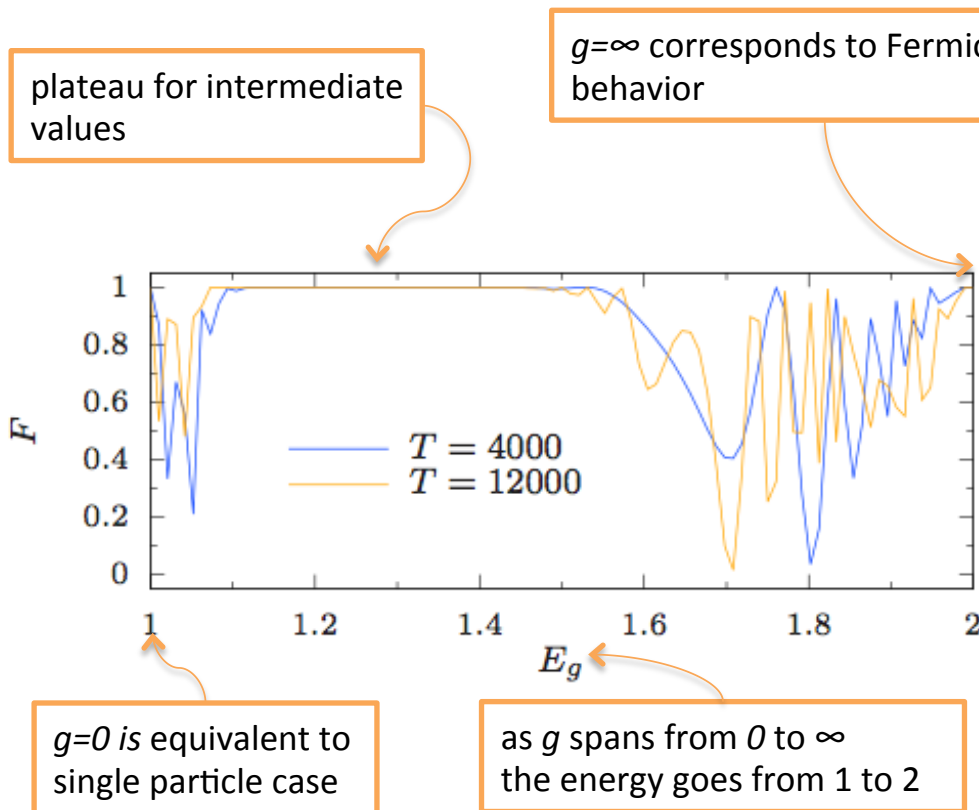


Transfer fidelity depends on the interaction strength g [2]

The Hamiltonian:

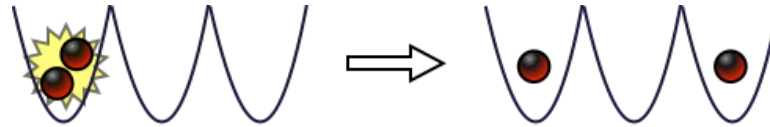
$$H = H_{01} + H_{02} + g\delta(x_1 - x_2)$$

Resonance is no longer guaranteed due to interaction term

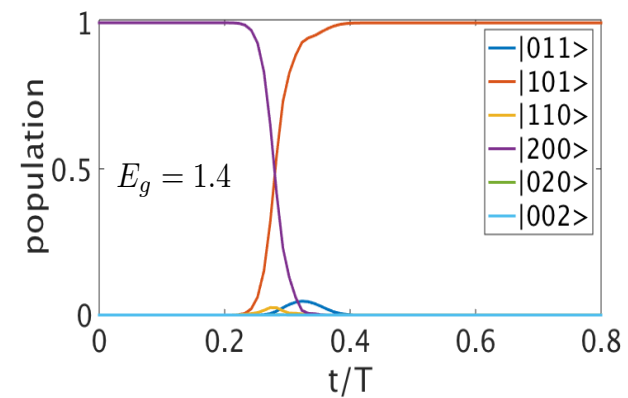
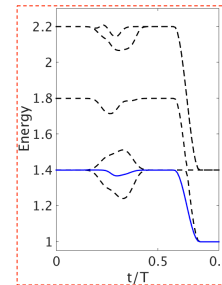
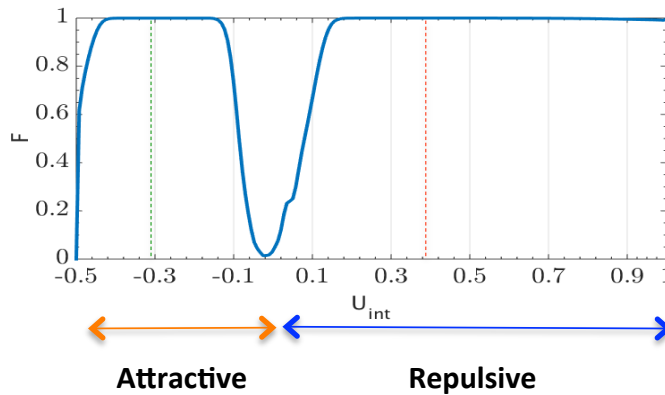
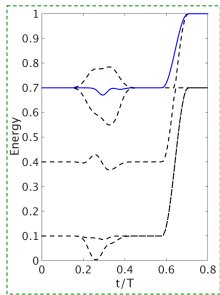
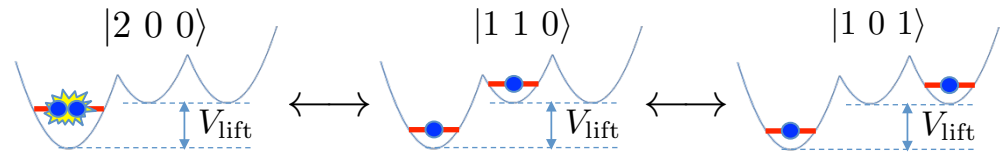


Beyond transport: particle separation

$$|2\ 0\ 0\rangle \rightarrow |1\ 0\ 1\rangle$$



Lift the traps while moving them to compensate for the interaction energy

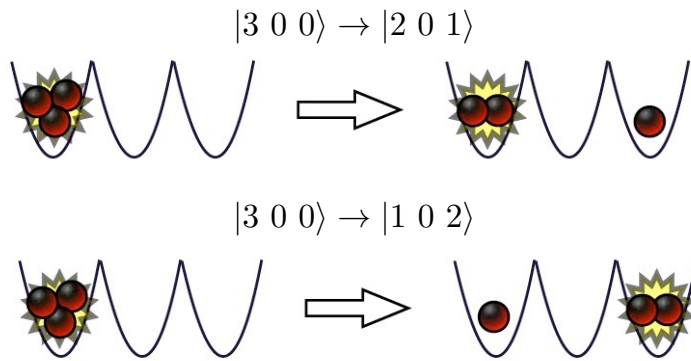


Separating more particles

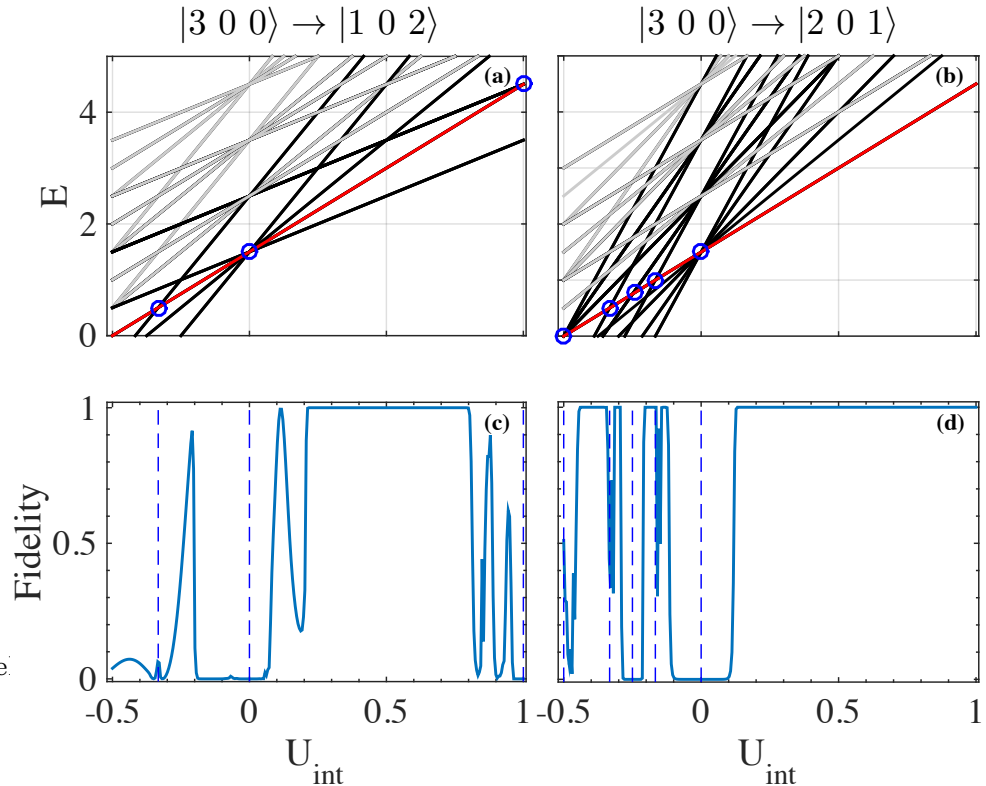
$$|\psi_{\text{init}}\rangle = |N \ 0 \ 0\rangle \rightarrow |\psi_{\text{target}}\rangle = |M \ 0 \ (N - M)\rangle$$

$$V_{\text{lift}} = MU_{\text{int}}$$

Does not depend on the total number of particles!



$$\hat{H}_{\text{BH}} = \hbar\omega \sum_{j=0}^{m_L-1} \left(j + \frac{1}{2}\right) \hat{N}_j^{\text{level}} + \sum_{i=1}^3 V_i \hat{N}_i^{\text{trap}} + \frac{U_{\text{int}}}{2} \sum_{i=1}^3 \hat{N}_i^{\text{trap}} (\hat{N}_i^{\text{trap}} - 1) + H_{\text{tunne}}$$



Experimental realization proposal and more details:

"A robust boson dispenser: Quantum state preparation in interacting many-particle systems", I. Reshodko, A. Benseny, Th. Busch, arXiv:1703.02189