

Numerical Libraries

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Overview

- Modular programming
- Libraries
- Module systems
- Scientific libraries
- Examples using GSL and cuFFT

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Don't reinvent the wheel!

Modular programming

Motivation

- Scientific software can be large, complex and subtle.
- Interactions grow as (number of lines of code)².
- You're either recoding the same thing, or are copy-pasting with a large risk of mistakes.

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- Design the interface (header files in C++, interface in Fortran).
- Implementation is separate (ideally separate file).
- Enforce boundaries. **Avoid global variables!** Use namespaces where needed (C++).

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Advantages

- Allows each module to be tested individually.
- Makes rebuilding software more efficient.
- Modifying code becomes easier, and version control more powerful.

Modular programming, compiling and linking

- In modular programming, several object files for different modules need to be linked together.
- In the example below, `app.cpp/app.f90` contains the main program and `alibrary.cpp/alibrary.h/alibraryf.f90/alibraryf.mod` are a C++ and f90 module.

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```
g++ -g -O2 -c -o app.o app.cpp
g++ -g -O2 -c -o alibrary.o alibrary.cpp
g++ -g app.o alibrary.o -o cppapp

gfortran -g -O2 -c -o app.o app.f90
gfortran -g -O2 -c -o alibraryf.o alibraryf.f90
gfortran -g app.o alibraryf.o -o f90app
```

(by the way, please use make or cmake in real life).

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gfortran -g -O2 -c -o app.o app.f90
gfortran -g -O2 -c -o alibraryf.o alibraryf.f90
gfortran -g app.o alibraryf.o -o f90app
```

(by the way, please use make or cmake in real life).

- What if we could use our `alibrary` in another project called `newapp`, without recompiling `alibrary.cpp` or `alibraryf.f90`?

From modular programming to libraries

From modular programming to libraries

- Copy .o and .h to separate directories:

```
alibrary.h      -> /base/include/alibrary.h  
alibraryf.mod  -> /base/include/alibraryf.mod  
alibrary.o     -> /base/lib/alibrary.o  
alibraryf.o    -> /base/lib/alibraryf.o
```

From modular programming to libraries

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alibrary.h      -> /base/include/alibrary.h
alibraryf.mod   -> /base/include/alibraryf.mod
alibrary.o      -> /base/lib/alibrary.o
alibraryf.o     -> /base/lib/alibraryf.o
```

- Must let compiler know where they are:

Add **-I** flag for include directories.

Absolute path for object file (*only for now!*).

```
g++ -g -O2 -I/base/include -c -o newapp.o newapp.cpp
g++ -g -o newapp newapp.o /base/lib/alibrary.o
```

```
gfortran -g -O2 -I/base/include -c -o newf90app.o newf90app.f90
gfortran -g -o newf90app newf90app.o /base/lib/alibraryf.o
```

Building with Libraries

Real libraries are similar; they have

- to be installed (and perhaps built first)
- header files (.h or .hpp) or module files (.mod) in some folder
- library files (object code) in a related folder.

Linux: library filenames start with lib and end in .a or .so.

```
g++ -g -o cppapp cppapp.o /base/lib/liblibrary.a  
gfortran -g -o f90app f90app.o /base/lib/alibraryf.a
```

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```
g++ -g -o cppapp cppapp.o /base/lib/liblibrary.a  
gfortran -g -o f90app f90app.o /base/lib/alibraryf.a
```

Instead of giving the explicit path in linker command, we should specify:

- the path to the library's object using the **-L** option
- the object code using **-lNAME** (with a lower case letter **-l**)
- libraries should come after the object files that use them.

```
g++ -g -L/base/lib -o cppapp cppapp.o -llibrary  
gfortran -g -L/base/lib -o f90app f90app.o -llibraryf
```

More Notes on Libraries

- C++ standard libraries (`vector`, `cmath`, ...) do not need any `-l...`'s.
- There are **standard directories** for libraries that needn't be specified in `-I` or `-L` options (`/usr/include`, ...)
- Libraries installed through a package manager end up in standard paths; they just need `-l` options.
- You usually also do not need `-I` or `-L` for libraries accessed using the 'module load' command on the supercomputers.
- If you compile your own libraries in non-standard locations, you do need `-I` and `-L` options (as well as the `-lNAME` clause).

Example: MPI

```
$ mpicc -show
gcc -I/opt/intel/compilers_and_libraries_2019.3.199/linux/mpi/intel64/include
-L/opt/intel/compilers_and_libraries_2019.3.199/linux/mpi/intel64/lib/release
-L/opt/intel/compilers_and_libraries_2019.3.199/linux/mpi/intel64/lib
-Xlinker --enable-new-dtags -Xlinker -rpath -Xlinker
/opt/intel/compilers_and_libraries_2019.3.199/linux/mpi/intel64/lib/release
-Xlinker -rpath -Xlinker /opt/intel/compilers_and_libraries_2019.3.199/linux/mpi/intel64/lib
-lmpifort -lmpi -lrt -lpthread -Xlinker --enable-new-dtags -ldl
```

```
$ mpifc -show
gfortran -I/opt/intel/compilers_and_libraries_2019.3.199/linux/mpi/intel64/include/gfortran/4.8.0
-I/opt/intel/compilers_and_libraries_2019.3.199/linux/mpi/intel64/include
-L/opt/intel/compilers_and_libraries_2019.3.199/linux/mpi/intel64/lib/release
-L/opt/intel/compilers_and_libraries_2019.3.199/linux/mpi/intel64/lib
-Xlinker --enable-new-dtags -Xlinker -rpath -Xlinker
/opt/intel/compilers_and_libraries_2019.3.199/linux/mpi/intel64/lib/release
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```


Software modules

Software modules are a very common way to make software available on shared supercomputers.

```
$ module avail
----- /opt/modulefiles -----
abaqus/2016          abyss/2.0.2          anaconda/4.2.0-3.5.2
abaqus/2017          AI/anaconda2-5.1.0_gpu  anaconda2/5.1.0
Abinit/7.10.5        AI/anaconda3-5.1.0_gpu  anaconda2/5.2.0
Abinit/8.0.8b        AI/anaconda3-5.1.0_gpu.2018-08  anaconda3/2019.03
Abinit/8.4.3         AIPS/31DEC16           anaconda3/5.1.0
abyss/1.5.2          allpaths-lg/52488      anaconda3/5.2.0(default)
...
```

E.g. try `module avail openblas` and `module help openblas`
(and `module spider openblas` for systems using lmod).

Must first do a `module load MODULE` before compiling and before running.

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Compile from source code with a "base" or "prefix" directory.

Common installation procedure (but read documentation!):

```
$ ./configure --prefix=<BASE>
$ make
$ make install
```

```
$ cmake -DCMAKE_INSTALL_PREFIX=<BASE> ....
$ make
$ make install
```

You choose the <BASE>, but it should be a directory that you have write permission to, e.g., a subdirectory of your **\$HOME**.

Using libraries that are not in standard directories

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- Alternatively, you can omit these by setting some linux environment variables:

```
export CPATH="$CPATH:<BASE>/include"      # compiler looks here for include files
export LIBRARY_PATH="$LIBRARY_PATH:<BASE>/lib"  # and here for library files
export LD_LIBRARY_PATH="$LD_LIBRARY_PATH:<BASE>/lib" # runtime linker looks here
```

You either enter these commands on the linux prompt before compiling, or, to set these automatically when you log in, add these lines to the `.bashrc` file in your home folder.

- The last one (`LD_LIBRARY_PATH`) may be necessary to run the application, even when it was successfully built and linked already.

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- The last one (`LD_LIBRARY_PATH`) may be necessary to run the application, even when it was successfully built and linked already.
- If the library installs binary applications (i.e. commands) as well, you'll also need to set

```
export PATH="$PATH:<BASE>/bin"      # linux shell looks for executables here
```

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So many libraries, so little time...

Some libraries for scientific computing (CPU)

BLAS interface for libraries for basic linear algebra operations.

C C++ Fortran

LAPACK Linear solvers, eigenvalue problems, SVD, factorization. C C++ Fortran Python

ScaLAPACK Distributed version of LAPACK. C C++ Fortran

ARPACK-NG and **SLEPc** Eigenvalue problems. C C++ Fortran

Boost Peer-reviewed portable C++ source libraries C++

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Eigen Matrices, vectors, numerical solvers, ... C++

FFTW Fourier and related transforms. C C++ Fortran

HDF5 and **NetCDF** Portable data model, library, and file formats. C C++ Fortran

GSL Numerical analysis library. C C++

PETSc Scalable (parallel) solution of partial differential equations. C C++ Fortran

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PETSc Scalable (parallel) solution of partial differential equations. C C++ Fortran

Armadillo Matrix and vector maths similar to MATLAB. C++

Blaze Dense and sparse arithmetic. C++

Dlib Machine learning algorithms and tools. C++

MLpack Machine learning algorithms. C++ Python

Trilinos algorithms etc. for the solution of large-scale, complex multi-physics engineering and scientific problems. C C++

Eigenvalue solvers targeting exascale computers

ELPA

EigenExa

Some libraries for scientific computing (GPU)

cuBLAS / rocBLAS GPU-accelerated BLAS implementations

cuSOLVER / rocSOLVER^(β) / MAGMA GPU-accelerated LAPACK-like libraries

cuSPARSE / rocSPARSE GPU-accelerated sparse matrix libraries

cuFFT / rocFFT GPU-accelerated Fast Fourier Transforms libraries

cuRAND / rocRAND Random number generation on the GPU

NPP (CUDA) Performance primitives for image & video processing

Thrust GPU-accelerated STL-like library (parallel algorithms)

Some libraries for scientific computing (Python)

NumPy Faster arrays for Python. Mind all the lessons from the HPC Python programming session!

SciPy Provides many user-friendly and efficient numerical routines such as routines for numerical integration and optimization.

Numba JIT compilation of a subset of Python and NumPy code into fast machine code.

Pandas Tabular data manipulation and analysis.

scikit-learn (sklearn) Machine Learning in Python. Simple and efficient tools for data mining and data analysis.

TensorFlow & PyTorch Neural nets/deep learning libraries.

Stan, PyMC Statistical modelling, data analysis, and Bayesian predictions.

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- Integration, differentiation, interpolation, approximation
- Statistics, histograms, fitting
- Monte Carlo integration, simulated annealing
- ODEs
- Polynomials, permutations
- Special functions
- Vectors, matrices

Note: C library means we'll likely need to deal with some pointers and casts.

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#include <gsl/gsl_roots.h>
#include <gsl/gsl_errno.h>

struct Params {double v, w, a, b, c;};

double examplefunction(double x, void* param){
    auto [v, w, a, b, c] = *(Params*)param;
    return a*cos(sin(v+w*x))+b*x-c*x*x;
}

int main() {
    double x_lo = -4.0;
    double x_hi = 5.0;
    Params args = {0.3, 2./3., 2., 1./1.3, 1/30.};
    gsl_root_fsolver* solver;
    solver = gsl_root_fsolver_alloc(
        gsl_root_fsolver_brent);
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```
    gsl_function fwrapper;
    fwrapper.function = examplefunction;
    fwrapper.params = &args;
    gsl_root_fsolver_set(solver,&fwrapper,x_lo,x_hi);

    std::cout << "iter lower upper root err\n";
    int status, iter = 0;
    do {
        gsl_root_fsolver_iterate(solver);
        double x_rt = gsl_root_fsolver_root(solver);
        double x_lo = gsl_root_fsolver_x_lower(solver);
        double x_hi = gsl_root_fsolver_x_upper(solver);
        std::cout << iter++ << " " << x_lo << " " << x_hi
            << " " << x_rt << " " << x_hi-x_lo << "\n";
        status=gsl_root_test_interval(x_lo,x_hi,0,1e-8);
    } while (status==GSL_CONTINUE and iter < 100);
    gsl_root_fsolver_free(solver);
}
```

Compilation and linkage

- Lots of `gs1...` stuff.
- The rest is just wrappers, setting up parameters and calling the appropriate functions.
- There are pointers and typecasts, because we're dealing with a C library.

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Output

```
$ ./gslrx
iter lower      upper      root      err
0      -4        -1.27657   -1.27657   2.72343
1     -1.95919   -1.27657   -1.95919   0.682622
2     -1.75011   -1.27657   -1.75011   0.473542
3     -1.75011   -1.74893   -1.74893   0.001179
```


Compilation and linkage

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- The rest is just wrappers, setting up parameters and calling the appropriate functions.
- There are pointers and typecasts, because we're dealing with a C library.
- How to compile on the command line?
- Even existing solutions like the ones in GSL, can't really be used until you understand the algorithm at a high level.

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```

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Using a C or C++ library in Python

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No problem! Most numerical libraries have a Python ***API***.

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No problem! Most numerical libraries have a Python ***API***.

And you can create your own wrapper using PyBind11, ctypes, or SWIG.

PyBind11 example

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PyBind11 example

Suppose we want to use cuFFT to calculate a Fourier transform, but in Python.

We write a function in C++ that wraps around the library call, and use *PyBind11* to create a Python “package”, which we can import and use like any other.

GPU-based FFT functionality (via cuFFT or otherwise) is provided by some packages on PyPI.

PyBind11 example (pycufft.cu)

This is the wrapper, defining a C++ function, that calls the cuFFT C function.

```
#include <complex>
#include <cufft.h>
#include <vector>

std::vector<std::complex<float>>>
fft(const std::vector<float>& signal)
{
    const size_t size = signal.size();
    float *signal_d;
    cudaMalloc((void**)&signal_d,
               size*sizeof(float));
    cudaMemcpy(signal_d, signal.data(),
               size*sizeof(float), cudaMemcpyHostToDevice);
    float2 *result_d;
    cudaMalloc((void**)&result_d,
               (size/2+1)*sizeof(float2));
    cufftHandle plan;
    cufftPlan1d(&plan, size, CUFFT_R2C, 1);
    cufftExecR2C(plan, (cufftReal*)signal_d,
                 (cufftComplex*)result_d);
```


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#include <complex>
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#include <vector>

std::vector<std::complex<float>>
fft(const std::vector<float>& signal)
{
    const size_t size = signal.size();
    float *signal_d;
    cudaMalloc((void**)&signal_d,
        size*sizeof(float));
    cudaMemcpy(signal_d, signal.data(),
        size*sizeof(float), cudaMemcpyHostToDevice);
    float2 *result_d;
    cudaMalloc((void**)&result_d,
        (size/2+1)*sizeof(float2));
    cufftHandle plan;
    cufftPlan1d(&plan, size, CUFFT_R2C, 1);
    cufftExecR2C(plan, (cufftReal*)signal_d,
        (cufftComplex*)result_d);
```

```
std::vector<std::complex<float>>
result(size/2+1);
cudaMemcpy(result.data(), result_d,
    (size/2+1)*sizeof(float2),
    cudaMemcpyDeviceToHost);
cudaFree(signal_d);
cudaFree(result_d);
cufftDestroy(plan);
return result;
}

#include <pybind11/pybind11.h>
#include <pybind11/stl.h>
#include <pybind11/complex.h>
PYBIND11_MODULE(pycufft, m) {
    m.doc() = "cuFFT wrapper";
    m.def("fft", &fft, "docstring");
}
```

PyBind11 example (pycufft_example.py)

This is an example of a Python script using our wrapped library.

```
import pycufft, numpy as np
w0      = 5      # rad/s
t_max   = 20     # s
n        = 2048
t = np.linspace(0, t_max, n)
x = np.sin(w0*t)
result = pycufft.fft(x)
mag = np.abs(result)
w_recovered = mag.argmax() * 2*np.pi/t_max
print(f'Recovered angular frequency: {w_recovered} rad/s')
```

Note that the return type of our wrapped function is a list, we can ask PyBind11 to return a NumPy array, but that doesn't fit on one slide

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(1) Copy code for Python session if you haven't done so already:

```
cp -r /jet/home/rzon/hpcpycode ~
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```

(3) Load the CUDA module and compile the shared object file:

```
module load cuda
nvcc -O3 -shared -std=c++17 -Xcompiler="-Wall -fPIC" \
$(python3 -m pybind11 --includes) pycufft.cu \
-o pycufft.cpython-38-x86_64-linux-gnu.so -lcufft
```

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nvcc -O3 -shared -std=c++17 -Xcompiler="-Wall -fPIC" \
$(python3 -m pybind11 --includes) pycufft.cu \
-o pycufft.cpython-38-x86_64-linux-gnu.so -lcufft
```

(4) Try running the script:

```
srun --partition=GPU-shared --gres=gpu:v100-32:1 \
--time=00:01:00 python pycufft_example.py
```

Final remarks

- “Do not reinvent the wheel”, i.e. reuse libraries already developed.
- Use **mature** libraries, well-known in the corresponding field/community. They have been developed, maintained, debugged, tested, ...
- Optimized and really good at the task(s) in question.
- Libraries are a cornerstone element in modularity and professional software development.
- Consider including further elements of software engineering, such as, automation (via `make` or `cmake`) of compilation and linking – helps with compilation flags and cross-platform developments.